

Transformations Of Functions Cheat Sheet

Transformations of F(x) Cheat Sheet

Equation	What Happens to the Graph
$f(x) + k$	Translate k units up
$f(x) - k$	Translate k units down
$f(x+h)$	Translate h units left
$f(x-h)$	Translate h units right
$a \cdot f(x)$ if $a > 1$	Stretch Vertically
$a \cdot f(x)$ if $0 < a < 1$	Shrink Vertically
$f(a \cdot x)$ if $a > 1$	Shrink horizontally
$f(a \cdot x)$ if $0 < a < 1$	Stretch horizontally
$-f(x)$	Reflect over x axis
$f(-x)$	Reflect over y axis

$f(x) = a(x - h) + k$

Vertical Shifts
+k = move up
-k = move down

Horizontal Shifts
-h = move left
+h = move right

Vertical Stretch/Compression
a > 1 = stretch
0 < a < 1 = shrink

Transformations of functions cheat sheet are essential tools for students and professionals in mathematics, particularly in algebra and calculus. Understanding how to manipulate and transform functions is crucial for graphing, solving equations, and analyzing various mathematical models. This article serves as a comprehensive guide to the transformations of functions, detailing the various types of transformations, their effects on the graph of a function, and examples to clarify each concept.

Types of Transformations

Transformations of functions can be broadly categorized into four main types:

1. Vertical Shifts
2. Horizontal Shifts
3. Reflections
4. Stretches and Compressions

Let’s delve deeper into each of these categories.

1. Vertical Shifts

Vertical shifts involve moving the entire graph of a function up or down along the y-axis. This transformation is represented mathematically as follows:

- If $f(x)$ is the original function, then:
- $f(x) + k$ shifts the graph up by k units (where $k > 0$).
- $f(x) - k$ shifts the graph down by k units (where $k > 0$).

Example:

- For the function $f(x) = x^2$:
- $f(x) + 3 = x^2 + 3$ shifts the graph of $f(x)$ up by 3 units.
- $f(x) - 2 = x^2 - 2$ shifts the graph down by 2 units.

2. Horizontal Shifts

Horizontal shifts move the graph left or right along the x-axis. This transformation is represented mathematically as follows:

- If $f(x)$ is the original function, then:
- $f(x - h)$ shifts the graph right by h units (where $h > 0$).
- $f(x + h)$ shifts the graph left by h units (where $h > 0$).

Example:

- For the function $f(x) = x^2$:
- $f(x - 4) = (x - 4)^2$ shifts the graph right by 4 units.
- $f(x + 2) = (x + 2)^2$ shifts the graph left by 2 units.

3. Reflections

Reflections involve flipping the graph of a function over a specific axis. This transformation can be represented mathematically as follows:

- If $f(x)$ is the original function, then:
- $-f(x)$ reflects the graph over the x-axis.
- $f(-x)$ reflects the graph over the y-axis.

Example:

- For the function $f(x) = x^2$:
- $-f(x) = -x^2$ reflects the graph over the x-axis.
- $f(-x) = (-x)^2 = x^2$ reflects the graph over the y-axis (in this case, the graph does not change since it's symmetric).

4. Stretches and Compressions

Stretches and compressions alter the shape of the graph either vertically or horizontally. This transformation is represented mathematically as follows:

- Vertical stretches and compressions:
- $af(x)$ stretches the graph vertically by a factor of a (where $a > 1$) or compresses it

(where $(0 < a < 1)$).

- Horizontal stretches and compressions:

- $f(bx)$ compresses the graph horizontally by a factor of b (where $b > 1$) or stretches it (where $(0 < b < 1)$).

Example:

- For the function $f(x) = x^2$:

- $2f(x) = 2x^2$ vertically stretches the graph by a factor of 2.

- $0.5f(x) = 0.5x^2$ vertically compresses the graph by a factor of 0.5.

- $f(2x) = (2x)^2 = 4x^2$ horizontally compresses the graph by a factor of 2.

- $f(0.5x) = (0.5x)^2 = 0.25x^2$ horizontally stretches the graph by a factor of 2.

Combining Transformations

Transformations can be combined in various ways to create more complex effects on the function's graph. The order of transformations matters, so understanding how to apply them sequentially is crucial.

Order of Transformations

1. Horizontal shifts are applied first.
2. Stretches/compressions are applied next.
3. Reflections follow.
4. Vertical shifts are applied last.

Example:

Consider the function $f(x) = x^2$ and the transformation $g(x) = -2(x - 3)^2 + 4$.

- Step 1: Horizontal Shift: $(x - 3)$ moves the graph to the right by 3 units.

- Step 2: Vertical Stretch/Reflection: -2 reflects the graph over the x-axis and stretches it vertically by a factor of 2.

- Step 3: Vertical Shift: $+4$ moves the graph up by 4 units.

This results in a graph that is flipped, stretched, and positioned appropriately.

Common Functions and Their Transformations

To better understand transformations, let's look at some common functions and how they transform:

- Linear Function: $f(x) = x$

- Vertical Shift: $f(x) + 2$ shifts up by 2.

- Horizontal Shift: $f(x - 3)$ shifts right by 3.

- Reflection: $-f(x)$ reflects over the x-axis.

- Quadratic Function: $f(x) = x^2$
- Vertical Stretch: $3f(x) = 3x^2$ stretches vertically.
- Horizontal Compression: $f(0.5x) = (0.5x)^2$ stretches horizontally.
- Absolute Value Function: $f(x) = |x|$
- Vertical Shift: $f(x) - 1$ shifts down by 1.
- Reflection: $-f(x)$ reflects over the x-axis.
- Trigonometric Functions: $f(x) = \sin(x)$
- Vertical Stretch: $2\sin(x)$ stretches vertically by a factor of 2.
- Horizontal Shift: $\sin(x - \pi/2)$ shifts right by $\pi/2$.

Conclusion

The transformations of functions cheat sheet is a valuable resource for anyone studying mathematics. By mastering these transformations, individuals can gain a deeper understanding of how functions behave and interact with each other. Whether applied in algebra, calculus, or real-world scenarios, these transformations provide a framework for analyzing and solving complex problems. Remember to practice combining transformations and apply them to various functions to solidify your understanding.

Frequently Asked Questions

What are the basic types of transformations of functions?

The basic types of transformations include translations (shifts), reflections, stretches, and compressions.

How do you perform a vertical shift on a function?

To perform a vertical shift, you add or subtract a constant from the function. For example, $f(x) + k$ shifts the graph up by k units, while $f(x) - k$ shifts it down by k units.

What is the effect of a horizontal shift on a function?

A horizontal shift is achieved by adding or subtracting a constant inside the function's argument. For example, $f(x - h)$ shifts the graph to the right by h units, while $f(x + h)$ shifts it to the left by h units.

How do reflections affect the graph of a function?

Reflections can flip the graph over the x-axis or y-axis. To reflect over the x-axis, use $-f(x)$, and to reflect over the y-axis, use $f(-x)$.

What are vertical and horizontal stretches and compressions?

A vertical stretch is achieved by multiplying the function by a factor greater than 1 (e.g., $af(x)$), while a vertical compression uses a factor between 0 and 1. A horizontal stretch uses a factor

greater than 1 in $f(kx)$ for $k < 1$, and a compression uses a factor between 0 and 1.

Can transformations be combined, and how does that work?

Yes, transformations can be combined. You apply the transformations in the following order: horizontal shifts, stretches/compressions, reflections, and vertical shifts.

Where can I find a transformations of functions cheat sheet?

A transformations of functions cheat sheet can often be found in math textbooks, educational websites, or as downloadable resources from educational platforms that specialize in math.

Find other PDF article:
<https://soc.up.edu.ph/54-tone/files?dataid=YAT91-0027&title=sociology-john-j-macionis.pdf>

Transformations Of Functions Cheat Sheet

Transformations of Functions Cheat Sheet - PDF
Jun 30, 2023 · This cheat sheet provides a comprehensive overview of the various transformations that can be applied to functions, including translations, stretches, compressions, and reflections.

Transformations of Functions Cheat Sheet - PDF
Aug 4, 2021 · 2014 CTM Radio Lab This cheat sheet provides a comprehensive overview of the various transformations that can be applied to functions, including translations, stretches, compressions, and reflections.

Transformations of Functions Cheat Sheet - PDF
Mar 1, 2017 · This cheat sheet provides a comprehensive overview of the various transformations that can be applied to functions, including translations, stretches, compressions, and reflections.

Transformations of Functions Cheat Sheet - PDF
May 14, 2024 · 226 227 228 229 230 231 232 233 234 235 This cheat sheet provides a comprehensive overview of the various transformations that can be applied to functions, including translations, stretches, compressions, and reflections.

Transformations of Functions Cheat Sheet - PDF
Aug 29, 2022 · This cheat sheet provides a comprehensive overview of the various transformations that can be applied to functions, including translations, stretches, compressions, and reflections.

Transformations of Functions Cheat Sheet (10) - PDF
Apr 5, 2025 · This cheat sheet provides a comprehensive overview of the various transformations that can be applied to functions, including translations, stretches, compressions, and reflections.

Transformations of Functions Cheat Sheet - ZCOOL
This cheat sheet provides a comprehensive overview of the various transformations that can be applied to functions, including translations, stretches, compressions, and reflections.

Transformations of Functions Cheat Sheet - PDF
This cheat sheet provides a comprehensive overview of the various transformations that can be applied to functions, including translations, stretches, compressions, and reflections.

Transformations of Functions Cheat Sheet - PDF

[illegible]

“ ” -36

Nov 30, 2023 · ...

Login | Salesforce

Salesforce Customer Secure Login Page. Login to your Salesforce Customer Account.

The Number 1 CRM Software | Salesforce Canada

What is Salesforce? Salesforce brings together all your data, from any source, so you can act on it with trusted AI and ...

What is Salesforce? | What does Salesforce do?

What does Salesforce do? Salesforce helps you stay ahead of changing customer expectations with data tools, trusted and autonomous AI, and best ...

Salesforce - Wikipedia

Salesforce was founded on March 8, 1999 by former Oracle executive Marc Benioff, together with Parker Harris, Dave Moellenhoff, and Frank Dominguez as ...

Trailhead | The fun way to learn

Everyone can learn Salesforce. Whether you are an admin, user, or developer, there is a trail for you.

Unlock the secrets of function transformations with our comprehensive cheat sheet! Master shifts

[Back to Home](#)