Piecewise Functions Answer Key

Piecewise Functions

Sketch the graph of each function.

1) $f(x) = \begin{cases} -2x - 1, & x \le 2 \\ -x + 4, & x > 2 \end{cases}$

2) $f(x) = \begin{cases} -4, & x \le -2 \\ x - 2, & -2 < x < 2 \\ -2x + 4, & x \ge 2 \end{cases}$

3) $f(x) = \begin{cases} -2^x, & x < -4 \\ -|x|, & -4 \le x \le 0 \\ 4 - x^2, & x > 0 \end{cases}$
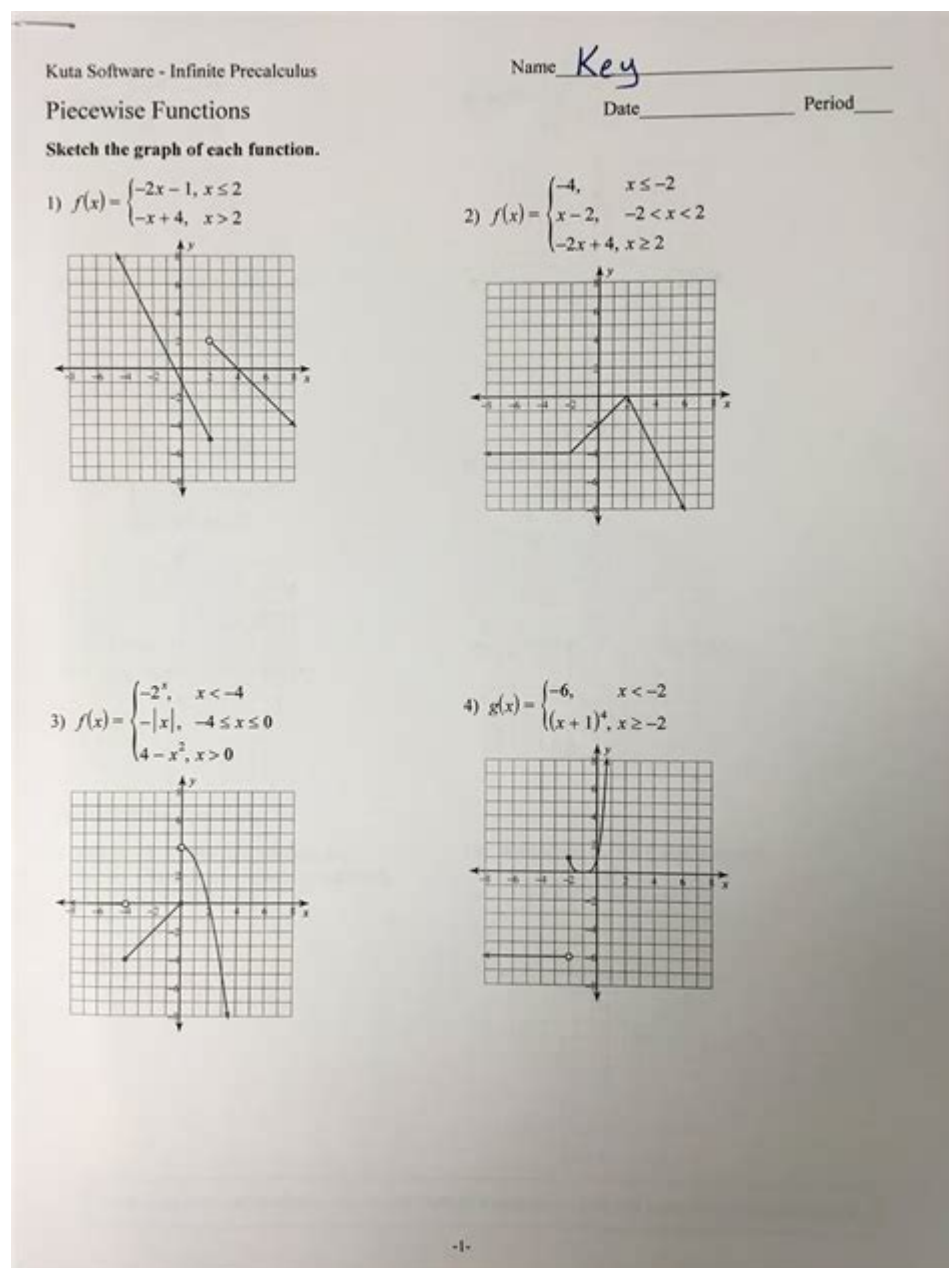
4) $g(x) = \begin{cases} -6, & x < -2 \\ (x + 1)^4, & x \ge -2 \end{cases}$

Piecewise functions answer key are essential tools in mathematics that help in understanding how different functions can be defined over different intervals. These functions are composed of multiple sub-functions, each applying to a specific interval of the input variable. In this article, we will explore the definition, properties, and applications of piecewise functions, as well as provide an answer key to common problems related to them.

What is a Piecewise Function?

A piecewise function is defined by different expressions depending on the value of the input variable. This allows for flexibility in defining functions that may behave differently across various intervals. The general

form of a piecewise function can be written as follows:

$$
f(x) =
\begin{cases}
f_1(x) & \text{if } x < a \\
f_2(x) & \text{if } a \leq x < b \\
f_3(x) & \text{if } x \geq b
\end{cases}
$$

In this notation:
- $f_1(x)$, $f_2(x)$, and $f_3(x)$ are different functions or expressions.
- a and b are the boundaries that dictate which function to use.

Characteristics of Piecewise Functions

Understanding the characteristics of piecewise functions is crucial for working with them effectively. Here are some key features:

Continuity

- A piecewise function can be continuous at a point where its sub-functions meet, provided the limits from both sides match the value of the function at that point.
- If the limits do not match, the function is considered discontinuous at that point.

Domain

- The domain of a piecewise function is the union of the domains of the individual pieces.
- It is essential to specify the intervals clearly to avoid confusion.

Range

- The range of a piecewise function is determined by the outputs of the sub-functions over their respective intervals.
- It's often necessary to evaluate each piece to find the overall range.

Applications of Piecewise Functions

Piecewise functions have various applications across different fields. Here are a few notable examples:

- **Economics:** Used to model different pricing strategies based on quantity

or demand.

- **Physics:** Employed in scenarios where an object's behavior changes, such as a ball thrown upwards and then falling.

- **Computer Science:** Used in algorithms that require different procedures based on conditions.

- **Statistics:** Useful in defining probability distributions with different behaviors for different ranges.

Common Problems Involving Piecewise Functions

To understand how to work with piecewise functions, it is helpful to look at some common problems. Here are a few examples along with their solutions:

Example 1: Evaluating a Piecewise Function

Consider the piecewise function defined as follows:

$$
f(x) =
\begin{cases}
2x + 3 & \text{if } x < 1 \\
-x + 5 & \text{if } 1 \leq x < 3 \\
4 & \text{if } x \geq 3
\end{cases}
$$

Question: What is $f(0)$, $f(2)$, and $f(4)$?

Answer Key:
- To find $f(0)$: Since $0 < 1$, we use the first piece $f(0) = 2(0) + 3 = 3$.
- To find $f(2)$: Since $1 \leq 2 < 3$, we use the second piece $f(2) = -2 + 5 = 3$.
- To find $f(4)$: Since $4 \geq 3$, we use the third piece $f(4) = 4$.

Thus, $f(0) = 3$, $f(2) = 3$, and $f(4) = 4$.

Example 2: Finding the Domain and Range

Let's take the same piecewise function from Example 1.

Question: What is the domain and range of $f(x)$?

Answer Key:
- Domain: The function is defined for all real numbers because it covers all intervals: $(-\infty, 1) \cup [1, 3) \cup [3, \infty) $.
- Range:
- From the first piece $2x + 3$ as x approaches 1 from the left, $f(1)$

= 5\).
- From the second piece \(-x + 5\) at \(x = 1\), \(f(1) = 4\) and approaches \(2\) as \(x\) approaches \(3\).
- The third piece is constant \(4\).

Thus, the range is \([2, 5]\).

Example 3: Graphing a Piecewise Function

Question: Graph the piecewise function from Example 1.

Answer Key:
1. For \(x < 1\), graph the line \(y = 2x + 3\) with an open circle at \((1, 5)\).
2. For \(1 \leq x < 3\), graph the line \(y = -x + 5\) with a closed circle at \((1, 4)\) and an open circle at \((3, 2)\).
3. For \(x \geq 3\), graph the horizontal line \(y = 4\) starting from \((3, 4)\) and extending to the right.

Conclusion

In summary, piecewise functions answer key provide a comprehensive approach to understanding and solving problems involving piecewise functions. By mastering the evaluation, domain, range, and graphing techniques of these functions, students and professionals alike can apply them effectively in various mathematical and real-world contexts. Remember, practice is key to gaining confidence in working with piecewise functions, so explore numerous problems to solidify your understanding.

Frequently Asked Questions

What are piecewise functions?

Piecewise functions are functions that are defined by different expressions or formulas over different intervals of their domain.

How do you evaluate a piecewise function at a specific point?

To evaluate a piecewise function at a specific point, you first determine which interval the point falls into and then use the corresponding expression for that interval.

What is the importance of the domain in piecewise functions?

The domain in piecewise functions is crucial as it specifies the intervals over which each piece of the function is valid, ensuring that the function is properly defined.

Can piecewise functions be continuous?

Yes, piecewise functions can be continuous if the pieces connect at their endpoints without any gaps or jumps.

How do you graph a piecewise function?

To graph a piecewise function, plot each piece according to its defined interval, ensuring to check whether to include or exclude endpoints based on the function's definitions.

Find other PDF article:

Piecewise Functions Answer Key

Tires, Oil Changes & Brakes | Firestone Complete Auto Care
From a new set of tires to an oil change, alignment to brakes, we're the complete auto repair package that's committed to helping keep your car running newer longer.

Firestone Complete Auto Care - Repair & Service ...
Firestone Complete Auto Care is here to service and repair your vehicle, from the engine to the exhaust system. We're also here to provide you with the information you need to make the ...

Find A Firestone Complete Auto Care Near You

Find Firestone Complete Auto Care tire places near me for excellent auto repair and service by highly qualified technicians. View store hours, offers, and more!

Car Repair & Tires in Pittsburgh, PA | Firestone Complete Auto Care
Turn to your local Firestone Complete Auto Care for the right car services in Pittsburgh, PA. Make your appointment for tires, brakes, batteries, and more.

Asheville, NC - 85 Tunnel Rd - Firestone Complete Auto Care

Find expert auto care at 85 Tunnel Rd in Asheville, NC. From tires to repairs, Firestone Complete Auto Care has the services your vehicle needs.

Vehicle Service at Firestone Complete Auto Care

Help your car run better, longer. Get tire, maintenance, service, and repair recommendations for your make, model, and year from Firestone Complete Auto Care.

Schedule Appointment | Firestone Complete Auto Care

Get Coupons > Firestone Credit Card Apply Now Manage Your Credit Card My Firestone App

Car Repair & Tires in Orlando, FL | Firestone Complete Auto Care

Turn to your local Firestone Complete Auto Care for the right car services in Orlando, FL. Make your appointment for tires, brakes, batteries, and more.

Loveland, CO - 1383 Sculptor Dr - Firestone Complete Auto Care

Find expert auto care at 1383 Sculptor Dr in Loveland, CO. From tires to repairs, Firestone Complete Auto Care has the services your vehicle needs.

Virginia Car Repair & Tires | Firestone Complete Auto Care

Car problems big and small, you can turn to your local Firestone Complete Auto Care for the right automotive services and car repairs in Virginia.

Change email address of msi account - MSI Global English Fo...

May 13, 2021 · actually the email address can be changed by logging on to account.msi.com login page, then scroll down to the Account section and click …

Unable to log in to MSI account - MSI Global English Forum

Sep 6, 2021 · The rest all have you complete the accoutn login, which immedaitely takes you to the page telling you to activate your account first. So a …

MSI Global English Forum

Jul 17, 2025 · For you to discuss gaming related topics such as gaming events, your best settings, and etc. No Spam! …

Claw 8 AI+ update caused sound and gfx stuttering

Jun 4, 2025 · I updated the recommended Intel drivers + what Windows update was pushing. After installation, the device is not working while the 'Intel AI Boost' …

[Update] MSI Center M 2.0.2501.0601 Released (For Cla...

Jan 14, 2025 · New version have already been pushed via Live Update in MSI Center M, and will be available later for downloading on the official support …

Unlock the mystery of piecewise functions with our comprehensive answer key! Discover how to solve them effectively. Learn more for expert tips and solutions!

[Back to Home](#)