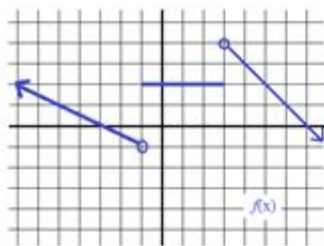
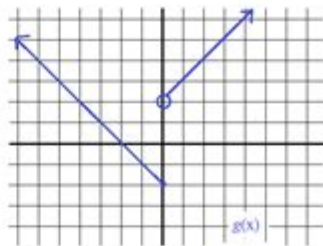


Piecewise Function Practice Problems

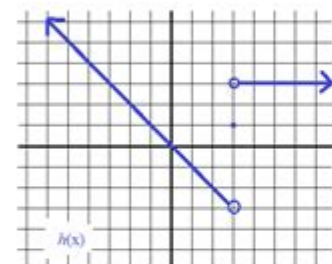
III. Identifying the Piecewise function -- write an expression to describe the graph



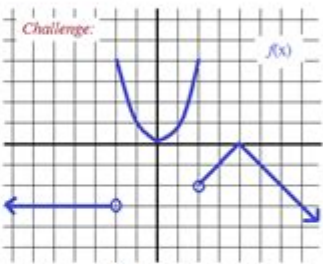
$$f(x) = \begin{cases} -1/2(x) - 3/2 & \text{if } x < -1 \\ 2 & \text{if } -1 \leq x \leq 3 \\ -x + 7 & \text{if } x > 3 \end{cases}$$



$$g(x) = \begin{cases} x + 2 & \text{if } x > 0 \\ -x - 2 & \text{if } x \leq 0 \end{cases}$$



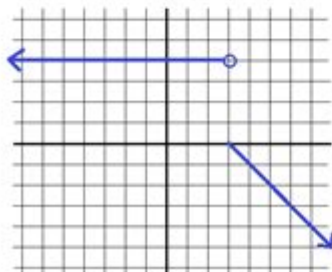
$$h(x) = \begin{cases} 3 & \text{if } x > 3 \\ 1 & \text{if } x = 3 \\ -x & \text{if } x < 3 \end{cases}$$



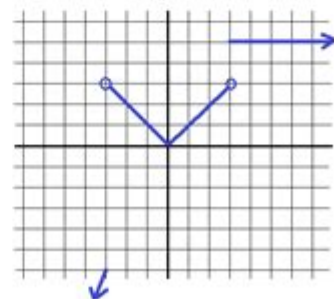
$$f(x) = \begin{cases} -3 & \text{if } x < -2 \\ x^2 & \text{if } -2 \leq x \leq 2 \\ -x - 4 & \text{if } x > 2 \end{cases}$$

IV. Graphing Piecewise functions

$$f(x) = \begin{cases} 4, & \text{if } x < 3 \\ -x + 3, & \text{if } x \geq 3 \end{cases}$$



$$g(x) = \begin{cases} 2x, & \text{if } x < -3 \\ |x|, & \text{if } -3 \leq x < 3 \\ 5, & \text{if } x \geq 3 \end{cases}$$



Piecewise function practice problems are an essential part of mathematics, especially in the study of functions and their applications. They allow us to define functions in different ways based on the input values, making them versatile tools for modeling real-world scenarios. Understanding piecewise functions is crucial for students as they encounter them in calculus, algebra, and various applied fields. This article will explore the definition of piecewise functions, their properties, and provide a range of practice problems, along with solutions and explanations to enhance comprehension.

Understanding Piecewise Functions

Piecewise functions are defined by multiple sub-functions, each corresponding to a specific interval of the independent variable. The general form of a

piecewise function can be expressed as follows:

$$f(x) = \begin{cases} f_1(x) & \text{if } x < a \\ f_2(x) & \text{if } a \leq x < b \\ f_3(x) & \text{if } x \geq b \end{cases}$$

In this representation:

- $f_1(x)$, $f_2(x)$, and $f_3(x)$ are different functions that apply to different segments of the domain.
- a and b are constants that denote the boundaries between the segments.

Example of a Piecewise Function

Consider the following piecewise function:

$$f(x) = \begin{cases} x^2 & \text{if } x < 0 \\ 2x + 1 & \text{if } 0 \leq x < 3 \\ 5 & \text{if } x \geq 3 \end{cases}$$

This function consists of three parts:

- For values of x less than 0, the function outputs x^2 .
- For values of x between 0 and 3, the function outputs $2x + 1$.
- For values of x greater than or equal to 3, the function outputs a constant value of 5.

Properties of Piecewise Functions

Understanding the properties of piecewise functions can greatly assist in solving problems that involve them. Here are some key properties:

1. **Continuity:** A piecewise function can be continuous or discontinuous. To determine continuity at the boundaries, the limits from both sides must equal the function value at that point.
2. **Differentiability:** A piecewise function can be differentiable or non-differentiable at the boundaries. A function is differentiable at a point if the derivative exists at that point.
3. **Domain and Range:** The domain of a piecewise function is the union of the domains of its sub-functions. The range is the union of their ranges as well.

4. Graphing: Graphing piecewise functions involves plotting each defined function over its respective interval and ensuring that the transition points are marked clearly.

Practice Problems

To solidify the understanding of piecewise functions, let's dive into some practice problems. Each problem will be followed by its solution and explanation.

Problem 1

Define the piecewise function:

$$g(x) = \begin{cases} 3x + 2 & \text{if } x < -1 \\ x^2 & \text{if } -1 \leq x < 2 \\ 4 - x & \text{if } x \geq 2 \end{cases}$$

1. Evaluate $g(-2)$
2. Evaluate $g(0)$
3. Evaluate $g(3)$

Solution 1

1. For $g(-2)$, since $-2 < -1$, we use the first piece:

$$g(-2) = 3(-2) + 2 = -6 + 2 = -4.$$

2. For $g(0)$, since 0 falls within $-1 \leq x < 2$, we use the second piece:

$$g(0) = 0^2 = 0.$$

3. For $g(3)$, since $3 \geq 2$, we use the third piece:

$$g(3) = 4 - 3 = 1.$$

Thus, the evaluations are:

- $g(-2) = -4$
- $g(0) = 0$
- $g(3) = 1$

Problem 2

Consider the function:

$$h(x) = \begin{cases} x - 1 & \text{if } x < 1 \\ 2 & \text{if } x = 1 \\ 3x + 2 & \text{if } x > 1 \end{cases}$$

1. Determine whether $h(x)$ is continuous at $x = 1$.
2. Find $h(-1)$, $h(1)$, and $h(2)$.

Solution 2

1. To check continuity at $x = 1$, we need to evaluate:
 - The left-hand limit: $\lim (x \rightarrow 1^-) h(x) = 1 - 1 = 0$.
 - The right-hand limit: $\lim (x \rightarrow 1^+) h(x) = 3(1) + 2 = 5$.
 - The function value: $h(1) = 2$.

Since the left-hand limit (0) does not equal the right-hand limit (5), $h(x)$ is discontinuous at $x = 1$.

2. Evaluate:
 - $h(-1)$: Since $-1 < 1$, we use the first piece: $h(-1) = -1 - 1 = -2$.
 - $h(1)$: $h(1) = 2$ (given).
 - $h(2)$: Since $2 > 1$, we use the third piece: $h(2) = 3(2) + 2 = 6 + 2 = 8$.

Thus, the results are:

- $h(-1) = -2$
- $h(1) = 2$
- $h(2) = 8$

Conclusion

Piecewise functions are powerful mathematical constructs that allow for complex modeling and problem-solving. Through practice problems and understanding their properties, students can develop a solid grasp of how to work with these functions effectively. As seen in the examples, evaluating piecewise functions requires careful attention to the defined intervals and the corresponding formulas. By practicing these problems, students can enhance their mathematical skills and prepare themselves for more advanced topics in calculus and beyond.

Frequently Asked Questions

What is a piecewise function and how is it different from a standard function?

A piecewise function is defined by different expressions or formulas over different intervals of its domain. Unlike standard functions that have a single formula for all inputs, piecewise functions can have multiple rules depending on the input value.

How do you determine the value of a piecewise function at a specific point?

To determine the value of a piecewise function at a specific point, identify which interval the input value falls into and then apply the corresponding formula from that interval to calculate the output.

What are some common real-world applications of piecewise functions?

Piecewise functions are often used in real-world applications such as tax brackets, shipping costs, and pricing models where different rates apply depending on the quantity or value.

How do you graph a piecewise function?

To graph a piecewise function, first identify the intervals and corresponding formulas. Plot each segment on the graph according to its defined interval, ensuring to use open or closed circles to indicate whether endpoints are included.

What strategies can be used to solve piecewise function practice problems?

To solve piecewise function practice problems, carefully read the definition of the function, evaluate the input to find the appropriate interval, apply the correct formula, and check for continuity or any specific conditions at the boundaries.

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