

# Derivatives Of Inverse Trig Functions Worksheet

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## Quiz & Worksheet - Calculating Derivatives of Inverse Trigonometric Functions

1. Evaluate.

$$\frac{d}{dx} (\sin^{-1}(x))$$

- ☐  $\frac{1}{\sqrt{1-x^2}}$
- ☐  $\frac{1}{\sqrt{1+x^2}}$
- ☐  $\frac{1}{\sqrt{x^2-1}}$
- ☐  $\frac{-1}{\sqrt{1+x^2}}$

2. Find the derivative of  $y(t)$ .

$$y(t) = \tan^{-1}(2t)$$

- ☐  $y'(t) = \frac{2}{4t^2 + 1}$
- ☐  $y'(t) = \frac{2}{t^2 + 1}$
- ☐  $y'(t) = \frac{2}{\sqrt{t^2 + 1}}$
- ☐  $y'(t) = \frac{4}{2t^2 + 1}$

3. Find  $f'(x)$ .

$$f(x) = x^2 + \cos^{-1}(x+1)$$

- ☐  $f'(x) = 2x - \frac{1}{\sqrt{-x^2-2x}}$
- ☐  $f'(x) = 2x - \frac{1}{\sqrt{1-x^2}}$
- ☐  $f'(x) = x^2 - \frac{1}{\sqrt{1-x^2}}$
- ☐  $f'(x) = 2x - \frac{1}{x}$

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## Derivatives of Inverse Trig Functions Worksheet

Understanding the derivatives of inverse trigonometric functions is an essential part of calculus, especially when dealing with problems requiring differentiation. Inverse trigonometric functions allow us to find angles when given a ratio of two sides of a right triangle, and they have useful applications in various fields such as physics, engineering, and even in everyday problem-solving scenarios. This article will delve into the derivatives of inverse trigonometric functions, present a comprehensive worksheet, and provide examples to solidify understanding.

# What Are Inverse Trigonometric Functions?

Inverse trigonometric functions are the inverse operations of the standard trigonometric functions. They provide a way to determine an angle when the sine, cosine, tangent, or other trigonometric values are known. The primary inverse trigonometric functions include:

- Arcsine ( $\sin^{-1}$  or  $\arcsin$ )
- Arccosine ( $\cos^{-1}$  or  $\arccos$ )
- Arctangent ( $\tan^{-1}$  or  $\arctan$ )
- Arccotangent ( $\cot^{-1}$  or  $\operatorname{arccot}$ )
- Arcsecant ( $\sec^{-1}$  or  $\operatorname{arcsec}$ )
- Arccosecant ( $\csc^{-1}$  or  $\operatorname{arccsc}$ )

Each of these functions corresponds to their respective trigonometric functions, and they are defined on specific intervals to ensure the function is one-to-one.

## Derivatives of Inverse Trigonometric Functions

The derivatives of the inverse trigonometric functions can be derived using implicit differentiation or found in standard calculus textbooks. Here are the derivatives for each of the primary inverse trigonometric functions:

### 1. Arcsine Function

The derivative of the arcsine function is given by:

$$\frac{d}{dx}(\sin^{-1}(x)) = \frac{1}{\sqrt{1-x^2}}, \quad \text{for } -1 < x < 1$$

\]

## 2. Arccosine Function

The derivative of the arccosine function is:

\[

$$\frac{d}{dx}(\cos^{-1}(x)) = -\frac{1}{\sqrt{1-x^2}}, \quad \text{for } -1 < x < 1$$

\]

## 3. Arctangent Function

The derivative of the arctangent function is:

\[

$$\frac{d}{dx}(\tan^{-1}(x)) = \frac{1}{1+x^2}, \quad \text{for all } x$$

\]

## 4. Arccotangent Function

The derivative of the arccotangent function is:

\[

$$\frac{d}{dx}(\cot^{-1}(x)) = -\frac{1}{1+x^2}, \quad \text{for all } x$$

\]

## 5. Arcsecant Function

The derivative of the arcsecant function is:

$$\frac{d}{dx}(\sec^{-1}(x)) = \frac{1}{|x| \sqrt{x^2 - 1}}, \quad \text{for } |x| > 1$$

## 6. Arccosecant Function

The derivative of the arccosecant function is:

$$\frac{d}{dx}(\csc^{-1}(x)) = -\frac{1}{|x| \sqrt{x^2 - 1}}, \quad \text{for } |x| > 1$$

## Creating a Worksheet

A worksheet focused on the derivatives of inverse trigonometric functions would typically include several types of problems, such as direct derivative calculation, application problems, and verification tasks. Here's a structured worksheet you can use:

### Worksheet Problems

1. Find the Derivative: Calculate the derivative of the following functions:

- a)  $y = \sin^{-1}(2x)$
- b)  $y = \cos^{-1}(x^2 - 1)$

- c)  $y = \tan^{-1}\left(\frac{x}{3}\right)$
- d)  $y = \cot^{-1}(5 - x)$
- e)  $y = \sec^{-1}(x^3)$
- f)  $y = \csc^{-1}(2x + 1)$

2. Application Problems: Solve the following word problems involving inverse trigonometric functions:

- a) A ladder leans against a wall forming an angle with the ground. If the foot of the ladder is 4 feet away from the wall, and the top of the ladder touches the wall at a height of 3 feet, find the angle the ladder makes with the ground.
- b) A person standing 30 meters away from a tree observes the top of the tree at an angle of elevation of 45 degrees. Calculate the height of the tree using inverse tangent.

3. Verification Tasks: Verify the derivatives of the following functions using the chain rule:

- a)  $y = \sin^{-1}(x^2 + 1)$
- b)  $y = \tan^{-1}\left(\frac{1}{x}\right)$

## Examples and Solutions

To better understand the application of derivatives of inverse trigonometric functions, consider some worked-out examples from the worksheet.

### Example 1: Finding the Derivative of $y = \sin^{-1}(2x)$

Using the chain rule, we have:

$$\frac{d}{dx} \sin^{-1}(2x) = \frac{1}{\sqrt{1 - (2x)^2}} \cdot 2 = \frac{2}{\sqrt{1 - 4x^2}}, \quad \text{where } |2x| < 1$$

Thus, the derivative is:

$$\frac{dy}{dx} = \frac{1}{\sqrt{1 - u^2}} \cdot \frac{du}{dx}$$

Calculating  $\left( \frac{du}{dx} = 2 \right)$ , we find:

$$\frac{dy}{dx} = \frac{2}{\sqrt{1 - (2x)^2}} = \frac{2}{\sqrt{1 - 4x^2}}, \quad -\frac{1}{2} < x < \frac{1}{2}$$

## Example 2: Application Problem

In the ladder problem, we utilize the arctangent function to find the angle  $\left( \theta \right)$ :

$$\theta = \tan^{-1}\left(\frac{3}{4}\right)$$

This gives us the angle formed by the ladder with the ground.

## Conclusion

The derivatives of inverse trigonometric functions are a vital component of calculus, providing tools for solving a variety of mathematical problems. Whether you are working through derivatives, applying them to real-world scenarios, or verifying results, understanding these concepts is essential. By using worksheets and example problems, students can enhance their comprehension and skill in handling derivatives of inverse trigonometric functions, preparing them for more advanced topics in calculus and

its applications.

## Frequently Asked Questions

### What are the basic derivatives of inverse trigonometric functions?

The basic derivatives are:  $\frac{d}{dx}(\arcsin(x)) = \frac{1}{\sqrt{1-x^2}}$ ,  $\frac{d}{dx}(\arccos(x)) = -\frac{1}{\sqrt{1-x^2}}$ ,  $\frac{d}{dx}(\arctan(x)) = \frac{1}{1+x^2}$ ,  $\frac{d}{dx}(\text{arccot}(x)) = -\frac{1}{1+x^2}$ ,  $\frac{d}{dx}(\text{arcsec}(x)) = \frac{1}{(|x|\sqrt{x^2-1})}$ , and  $\frac{d}{dx}(\text{arccsc}(x)) = -\frac{1}{(|x|\sqrt{x^2-1})}$ .

### How can I apply the chain rule to find the derivative of an inverse trig function?

To apply the chain rule, first identify the inner function and the outer inverse trig function. Use the derivative of the outer function and multiply it by the derivative of the inner function. For example, if  $y = \arcsin(g(x))$ , then  $\frac{dy}{dx} = \left(\frac{1}{\sqrt{1-g(x)^2}}\right) g'(x)$ .

### What types of problems can be solved using derivatives of inverse trig functions?

Problems such as finding the slopes of tangent lines, solving optimization problems, and analyzing the behavior of functions can be solved using derivatives of inverse trig functions. They are also useful in physics for modeling angles and rates of change.

### What is the significance of the domain and range of inverse trig functions when finding derivatives?

The domain and range of inverse trig functions are crucial because they determine the values for which the derivatives are defined. For instance,  $\arcsin(x)$  is defined for  $x$  in  $[-1, 1]$ , and its derivative is only real within this interval, which affects the overall behavior of the function.

## Can you provide an example of a problem involving the derivative of an inverse trig function?

Sure! For example, find the derivative of  $y = \arcsin(2x)$ . Using the chain rule,  $dy/dx = (1/\sqrt{1-(2x)^2}) \cdot 2 = 2/\sqrt{1-4x^2}$ , valid for  $x$  in  $[-1/2, 1/2]$ .

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