

# Derivatives Worksheet With Solution

Derivative Formulas      Worksheet      Name \_\_\_\_\_

Place the number of the basic derivative formula (1 - 26 from the sheet of Derivative Formulas) next to each derivative problem below (you do not need to solve the problem):

Given  $y = f(x)$ , determine  $\frac{dy}{dx}$  :

\_\_\_\_\_ 1.  $y = 8x$

\_\_\_\_\_ 2.  $y = \sin^3 2x$

\_\_\_\_\_ 3.  $y = xe^{\cos x}$

\_\_\_\_\_ 4.  $y = \sin^{-1}(x^3)$

\_\_\_\_\_ 5.  $y = \sin(\ln(x^3))$

\_\_\_\_\_ 6.  $y = \ln(x^2 - 5)$

\_\_\_\_\_ 7.  $y = 5$

\_\_\_\_\_ 8.  $y = \tan(3x^2)$

\_\_\_\_\_ 9.  $y = 3x^{-1} + 12x$

\_\_\_\_\_ 10.  $y = e^{\operatorname{Arctan}(x)}$

\_\_\_\_\_ 11.  $y = \tan^{-1}(\ln x)$

\_\_\_\_\_ 12.  $y = \sec^2(3x)$

\_\_\_\_\_ 13.  $y = \cot x$

\_\_\_\_\_ 14.  $y = x \cos\left(\frac{1}{x}\right)$

\_\_\_\_\_ 15.  $y = (e^2)^x$

\_\_\_\_\_ 16.  $y = e^{3x}$

\_\_\_\_\_ 17.  $y = e^e$

\_\_\_\_\_ 18.  $y = \frac{x^2}{e^{2x}}$

\_\_\_\_\_ 19.  $y = \ln(x) \sin(x)$

\_\_\_\_\_ 20.  $y = \ln(\sin(x))$

\_\_\_\_\_ 21.  $y = \tan^5(\ln(3x^2 + 3) + 8x)$

\_\_\_\_\_ 22.  $y = x^\pi$

\_\_\_\_\_ 23.  $y = \pi^x$

\_\_\_\_\_ 24.  $y = \pi^\pi$

\_\_\_\_\_ 25.  $y = x^x$

\_\_\_\_\_ 26.  $y = \frac{\sin(3x)}{\sqrt{x^2 - 5}}$

\_\_\_\_\_ 27.  $y = \cot^{-1}\left(\frac{1}{1+x^2}\right)$

\_\_\_\_\_ 28.  $y = 3x^2 - \cos^{-1}x$

**Derivatives worksheet with solution** is a crucial resource for students and professionals aiming to master the concept of derivatives in calculus. Derivatives form the backbone of differential calculus and are essential for understanding how functions behave. Whether you are preparing for a calculus exam, seeking to enhance your understanding, or looking to solve practical problems in physics, engineering, or economics, a derivatives worksheet can provide valuable practice and insights. This article will delve into the various aspects of derivatives, including their definitions, rules, and solutions to common problems, along with a comprehensive worksheet for practice.

# Understanding Derivatives

Derivatives represent the rate of change of a function with respect to its variable. In simpler terms, they tell us how a function is changing at any given point. The derivative of a function  $f(x)$  is denoted as  $f'(x)$  or  $\frac{df}{dx}$ .

## Definition

The formal definition of a derivative is given by the limit process:

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x + h) - f(x)}{h}$$

In this definition:

- $h$  is a small increment in  $x$ .
- The expression  $f(x + h) - f(x)$  represents the change in the function value.
- Dividing by  $h$  gives the average rate of change over the interval from  $x$  to  $x + h$ .
- Taking the limit as  $h$  approaches zero gives the instantaneous rate of change.

## Geometric Interpretation

Geometrically, the derivative of a function at a point gives the slope of the tangent line to the curve at that point. If the derivative is positive, the function is increasing; if it is negative, the function is decreasing.

## Rules of Differentiation

To solve derivative problems efficiently, understanding the fundamental rules of differentiation is essential. Below are some of the most commonly used rules:

### 1. Power Rule

If  $f(x) = x^n$ , where  $n$  is a constant, then:

$$f'(x) = nx^{n-1}$$

## 2. Product Rule

If  $f(x) = u(x)v(x)$ , then:

$$f'(x) = u'(x)v(x) + u(x)v'(x)$$

## 3. Quotient Rule

If  $f(x) = \frac{u(x)}{v(x)}$ , where  $v(x) \neq 0$ , then:

$$f'(x) = \frac{u'(x)v(x) - u(x)v'(x)}{(v(x))^2}$$

## 4. Chain Rule

If  $y = f(g(x))$ , then:

$$\frac{dy}{dx} = f'(g(x)) \cdot g'(x)$$

## 5. Basic Derivatives

Here are derivatives of some common functions:

- $\frac{d}{dx}(c) = 0$  where  $c$  is a constant.
- $\frac{d}{dx}(x) = 1$
- $\frac{d}{dx}(\sin x) = \cos x$
- $\frac{d}{dx}(\cos x) = -\sin x$
- $\frac{d}{dx}(\tan x) = \sec^2 x$
- $\frac{d}{dx}(e^x) = e^x$
- $\frac{d}{dx}(\ln x) = \frac{1}{x}$

## Derivatives Worksheet with Solutions

To solidify your understanding, here's a derivatives worksheet followed by its solutions.

## Worksheet Problems

1. Find the derivative of  $f(x) = 3x^4 - 5x^3 + 2x - 7$ .
2. Differentiate  $g(x) = x^2 \sin(x)$ .
3. Calculate the derivative of  $h(x) = \frac{x^2 + 1}{x - 1}$ .
4. If  $y = e^{2x} \cos(x)$ , find  $\frac{dy}{dx}$ .
5. Determine the derivative of  $k(x) = \ln(x^2 + 1)$ .

## Solutions

1. Solution to Problem 1:

$$f'(x) = 12x^3 - 15x^2 + 2$$

- Applying the power rule to each term.

2. Solution to Problem 2:

$$g'(x) = 2x \sin(x) + x^2 \cos(x)$$

- Using the product rule:  $u = x^2$  and  $v = \sin x$ .

3. Solution to Problem 3:

$$h'(x) = \frac{(2x)(x - 1) - (x^2 + 1)(1)}{(x - 1)^2} = \frac{x^2 - 2x - 1}{(x - 1)^2}$$

- Applying the quotient rule.

4. Solution to Problem 4:

$$\frac{dy}{dx} = 2e^{2x} \cos(x) - e^{2x} \sin(x)$$

- Using the product rule.

5. Solution to Problem 5:

$$k'(x) = \frac{2x}{x^2 + 1}$$

- Using the chain rule and the derivative of  $\ln(x)$ .

# Practice Makes Perfect

To truly grasp the concept of derivatives, practice is key. Here are some additional problems for you to tackle:

1. Differentiate  $m(x) = 5x^3 - 3x^2 + 4x + 1$ .
2. Find the derivative of  $n(x) = \tan(3x)$ .
3. Calculate  $p(x) = \sqrt{x^2 + 4}$ .
4. If  $q(x) = x^4 e^{-x}$ , find  $q'(x)$ .
5. Derive  $r(x) = \frac{1}{x^2 + 3}$ .

## Conclusion

Understanding and mastering derivatives through a derivatives worksheet with solutions is essential for anyone studying calculus. Derivatives not only help in solving mathematical problems but also have applications in various fields. By practicing the problems and reviewing the solutions, you will gain confidence in your ability to tackle more complex calculus challenges. As you progress, remember that the key to success in calculus is persistence and practice. Keep working through problems, and you'll soon find that derivatives become second nature.

## Frequently Asked Questions

### What is a derivative in calculus?

A derivative represents the rate of change of a function with respect to a variable. It is a fundamental concept in calculus that measures how a function changes as its input changes.

### How do you find the derivative of a polynomial function?

To find the derivative of a polynomial function, apply the power rule: multiply the coefficient by the exponent and subtract one from the exponent for each term.

### What is the difference between a derivative and a differential?

A derivative represents the slope of the tangent line to the function at a point, while a differential is an infinitesimal change in the variable, often expressed as 'dx' and 'dy' for small changes in x and y.

### Can you explain the product rule for derivatives?

The product rule states that if you have two functions  $u(x)$  and  $v(x)$ , the derivative of their

product is given by:  $(u v)' = u' v + u v'$ .

## What is the chain rule in finding derivatives?

The chain rule is used to differentiate composite functions. If  $y = f(g(x))$ , then the derivative is given by  $dy/dx = f'(g(x)) g'(x)$ .

## How do you solve a derivatives worksheet efficiently?

To solve a derivatives worksheet efficiently, first identify which rules apply to each function, work systematically through each problem, and double-check your calculations for accuracy.

## What are some common mistakes to avoid when calculating derivatives?

Common mistakes include forgetting to apply the rules correctly, misapplying the product or chain rule, neglecting to simplify the expressions, and making arithmetic errors.

## What are higher-order derivatives?

Higher-order derivatives are derivatives of derivatives. The first derivative gives the rate of change, the second derivative gives the rate of change of the rate of change, and so on.

## Where can I find resources for practicing derivatives?

Resources for practicing derivatives include online educational platforms, calculus textbooks, math problem-solving websites, and worksheets available for download from educational sites.

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