Composition Of Functions Worksheet Answers

Name: _____ Date: _____ Period: _____

COMPOSITE FUNCTION WORKSHEET

Directions: Show all work for credit. Work must be neat and answer must be circled.

For 1- 9: Let $f(x) = 2x - 1$, $g(x) = 3x$, and $h(x) = x^2 + 1$. Compute the following:

1. $f(g(-3))$

$g(-3) = 3(-3) = -9$

$f(-9) = 2(-9) - 1 = \boxed{-19}$

2. $f(h(7))$

$h(7) = (7)^2 + 1 = 49 + 1 = 50$

$f(50) = 2(50) - 1 = \boxed{99}$

3. $(g \circ h)(24)$

$h(24) = (24)^2 + 1 = 576 + 1 = 577$

$g(577) = 3(577) = \boxed{1731}$

4. $f(g(h(2)))$

$h(2) = (2)^2 + 1 = 4 + 1 = 5$

$g(5) = 3(5) = 15$

$f(15) = 2(15) - 1 = \boxed{29}$

5. $h(g(f(5)))$

$f(5) = 2(5) - 1 = 10 - 1 = 9$

$g(9) = 3(9) = 27$

$h(27) = (27)^2 + 1 = 729 + 1 = \boxed{730}$

6. $g(f(h(-6)))$

$h(-6) = (-6)^2 + 1 = 36 + 1 = 37$

$f(37) = 2(37) - 1 = 74 - 1 = 73$

$g(73) = 3(73) = \boxed{219}$

7. $f(x + 1)$

$f(x+1) = 2(x+1) - 1$

$= 2x + 2 - 1$

$= \boxed{2x + 1}$

8. $g(3a)$

$g(3a) = 3(3a)$

$= \boxed{9a}$

9. $h(x - 2)$

$h(x-2) = (x-2)^2 + 1$

$= (x-2)(x-2) + 1$

$= x^2 - 2x - 2x + 4 + 1$

$= \boxed{x^2 - 4x + 5}$

For 10-11: Let $f(x) = -3x + 7$ and $g(x) = 2x^2 - 8$. Compute the following:

10. $f(g(x)) = -3(2x^2 - 8) + 7$

$= -6x^2 + 24 + 7$

$= \boxed{-6x^2 + 31}$

11. $(g \circ f)(x) = 2(-3x + 7)^2 - 8$

$= 2(-3x + 7)(-3x + 7) - 8$

$= 2(9x^2 - 21x - 21x + 49) - 8$

$= 2(9x^2 - 42x + 49) - 8$

$= 18x^2 - 84x + 98 - 8$

$= \boxed{18x^2 - 84x + 90}$

12. If $f(x) = 3x - 5$ and $g(x) = x^2$, find $(f \circ g)(3)$

$g(3) = (3)^2 = 9$

$f(9) = 3(9) - 5 = \boxed{22}$

13. If $f(x) = -9x - 9$ and $g(x) = \sqrt{x - 9}$, find $(f \circ g)(10)$

$g(10) = \sqrt{10 - 9} = \sqrt{1} = 1$

$f(1) = -9(1) - 9 = -9 - 9 = \boxed{-18}$

Composition of functions worksheet answers can often be a source of confusion for students learning about functions in mathematics. Understanding how to compose functions and interpret their results is crucial for success in algebra and calculus. This article will explore the concept of function composition, provide examples, and present common problems with their answers to help clarify this important topic.

What is Function Composition?

Function composition is the process of combining two functions to produce a new function. If you have two functions, $f(x)$ and $g(x)$, the composition of these functions is denoted as $(f \circ g)(x)$, which means you apply g first and then f to the result of $g(x)$. The formal definition can be expressed as:

$$
(f \circ g)(x) = f(g(x))
$$

This means that you take the output of $g(x)$ and use it as the input for $f(x)$.

Understanding Function Notation

When dealing with function composition, it's essential to understand how to read and write function notation. Here are some key points:

1. Function Notation: The notation $f(x)$ represents a function f evaluated at x.
2. Composite Functions: The notation $(f \circ g)(x)$ indicates that you are composing two functions, f and g.
3. Order Matters: The order of composition is critical. $(f \circ g)(x)$ is not the same as $(g \circ f)(x)$.

Steps to Compose Functions

To compose functions, follow these steps:

1. Identify the two functions you want to compose.
2. Determine the order of composition (which function goes first).
3. Substitute the inner function into the outer function.
4. Simplify the resulting expression if possible.

Example of Function Composition

Let's consider two functions:

- $f(x) = 2x + 3$
- $g(x) = x^2$

To find $(f \circ g)(x)$:

1. We first evaluate $g(x)$:
$$
g(x) = x^2
$$
2. Next, substitute $g(x)$ into $f(x)$:
$$
f(g(x)) = f(x^2) = 2(x^2) + 3 = 2x^2 + 3
$$
3. Thus, $(f \circ g)(x) = 2x^2 + 3$.

Now, let's find $(g \circ f)(x)$:

1. Evaluate $f(x)$:
$$
f(x) = 2x + 3
$$
2. Substitute $f(x)$ into $g(x)$:
$$

G(F(x)) = G(2x + 3) = (2x + 3)^2
\]
3. Expanding this gives:
\[
G(F(x)) = 4x^2 + 12x + 9
\]
4. Thus, \((G \circ F)(x) = 4x^2 + 12x + 9 \).

Common Problems and Answers

To reinforce the understanding of function composition, let's look at some common problems along with their answers.

Problem 1

Given the functions:
- \(F(x) = x + 5 \)
- \(G(x) = 3x - 2 \)

Find \((F \circ G)(2) \).

Solution:

1. First, calculate \(G(2) \):
\[
G(2) = 3(2) - 2 = 6 - 2 = 4
\]
2. Now, substitute into \(F \):
\[
F(G(2)) = F(4) = 4 + 5 = 9
\]
3. Thus, \((F \circ G)(2) = 9 \).

Problem 2

Using the same functions, find \((G \circ F)(1) \).

Solution:

1. Calculate \(F(1) \):
\[
F(1) = 1 + 5 = 6
\]
2. Substitute into \(G \):
\[
G(F(1)) = G(6) = 3(6) - 2 = 18 - 2 = 16
\]
3. Thus, \((G \circ F)(1) = 16 \).

Problem 3

Let $(f(x) = x^3)$ and $(g(x) = \sqrt{x})$. Find $((f \circ g)(4))$ and $((g \circ f)(8))$.

Solution:

1. For $((f \circ g)(4))$:
- Calculate $(g(4))$:
$$
g(4) = \sqrt{4} = 2
$$
- Then substitute into (f):
$$
f(g(4)) = f(2) = 2^3 = 8
$$
So, $((f \circ g)(4) = 8)$.

2. For $((g \circ f)(8))$:
- Calculate $(f(8))$:
$$
f(8) = 8^3 = 512
$$
- Then substitute into (g):
$$
g(f(8)) = g(512) = \sqrt{512} = 16\sqrt{2}
$$
Thus, $((g \circ f)(8) = 16\sqrt{2})$.

Conclusion

Understanding the composition of functions is a vital skill in mathematics, particularly in algebra and calculus. By following the steps outlined in this article, and practicing with various functions and problems, students can become more comfortable with this concept. The provided problems and solutions serve as a valuable resource for reinforcing the principles of function composition. As students progress in their studies, mastering function composition will aid in their comprehension of more complex mathematical topics.

Frequently Asked Questions

What is a composition of functions?

A composition of functions is a combination of two functions where the output of one function becomes the input of another. It is denoted as $(f \circ g)(x) = f(g(x))$.

How do you find the composition of two functions?

To find the composition of two functions $f(x)$ and $g(x)$, substitute $g(x)$ into $f(x)$. For example, if $f(x) = 2x$ and $g(x) = x + 3$, then $(f \circ g)(x) = f(g(x)) = f(x + 3) = 2(x + 3) = 2x + 6$.

What are common mistakes when finding function compositions?

Common mistakes include not properly substituting the entire function, confusing the order of functions, and failing to simplify the final expression.

Can the composition of functions be commutative?

In general, function composition is not commutative; that is, (f ∘ g)(x) does not equal (g ∘ f)(x) for most function pairs.

What is the domain of a composition of functions?

The domain of the composition (f ∘ g)(x) is the set of all x in the domain of g such that g(x) is in the domain of f.

How can I check if my composition of functions is correct?

To check your composition, substitute a few values into the original functions and verify that the outputs match the outputs of your composed function.

Are there specific types of functions that are easier to compose?

Yes, linear functions, polynomial functions, and certain trigonometric functions often yield simpler compositions compared to more complex functions like logarithmic or exponential functions.

Where can I find worksheets for practicing compositions of functions?

Worksheets for practicing compositions of functions can be found on educational websites, math resource platforms, and through online searches for math worksheets or exercises.

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