

# Completing The Square Formula Algebra 2

Solving a Quadratic Equation by Completing the Square

$$\begin{array}{l} x^2 + 4x - 5 = 0 \\ \quad \quad +5 \quad +5 \\ x^2 + 4x = 5 \\ x^2 + 4x + 4 = 5 + 4 \\ (x+2)^2 = 9 \\ x+2 = \pm 3 \\ \quad \quad -2 \quad -2 \\ \hline x = \pm 3 - 2 \end{array} \qquad \begin{array}{l} \frac{4}{2} = 2 \\ 2^2 = 4 \\ x = 3 - 2 = 1 \\ x = -3 - 2 = -5 \end{array} \qquad x = \{-5, 1\}$$

**Completing the square formula algebra 2** is a vital technique in algebra that enables students to solve quadratic equations, transform quadratic functions, and analyze their properties more effectively. This method not only provides an alternative to the quadratic formula but also helps in understanding the vertex form of a parabola. In this article, we will delve into the process of completing the square, its applications, and the reasoning behind the technique, while also providing examples and practice problems for better comprehension.

## Understanding Quadratic Equations

Quadratic equations are polynomial equations of degree two, generally expressed in the standard form:

$$ax^2 + bx + c = 0$$

where  $a$ ,  $b$ , and  $c$  are constants, and  $a \neq 0$ . The solutions to these equations can be found using various methods, including factoring, using the quadratic formula, and completing the square.

## The Importance of Completing the Square

Completing the square serves several purposes in algebra:

1. **Finding Roots:** It allows us to rewrite the quadratic equation in a form that makes it easier to solve for the variable  $x$ .
2. **Graphing Quadratics:** It helps in converting the standard form of a quadratic function into vertex form, making it simpler to identify the vertex

and axis of symmetry.

3. Deriving the Quadratic Formula: The technique provides a foundation for deriving the quadratic formula from the standard form of a quadratic equation.

## The Process of Completing the Square

To complete the square, we follow a systematic approach. Here's a step-by-step guide:

### Step 1: Start with the Standard Form

Begin with the quadratic equation in standard form:

$$ax^2 + bx + c = 0$$

If  $a$  is not equal to 1, divide the entire equation by  $a$  to simplify:

$$x^2 + \frac{b}{a}x + \frac{c}{a} = 0$$

### Step 2: Move the Constant Term to the Other Side

Rearrange the equation by moving the constant term ( $\frac{c}{a}$ ) to the right side:

$$x^2 + \frac{b}{a}x = -\frac{c}{a}$$

### Step 3: Find the Value to Complete the Square

To complete the square, take half of the coefficient of  $x$  (which is  $\frac{b}{a}$ ), square it, and add it to both sides. The value to add is:

$$\left(\frac{b}{2a}\right)^2$$

So, the equation becomes:

$$x^2 + \frac{b}{a}x + \left(\frac{b}{2a}\right)^2 = -\frac{c}{a} + \left(\frac{b}{2a}\right)^2$$

## Step 4: Rewrite the Left Side as a Square

Now, the left side of the equation can be factored into a perfect square:

$$\left( x + \frac{b}{2a} \right)^2 = -\frac{c}{a} + \left( \frac{b}{2a} \right)^2$$

## Step 5: Solve for $x$

Finally, take the square root of both sides and solve for  $x$ :

$$x + \frac{b}{2a} = \pm \sqrt{-\frac{c}{a} + \left( \frac{b}{2a} \right)^2}$$

Subtract  $\left( \frac{b}{2a} \right)$  from both sides to isolate  $x$ :

$$x = -\frac{b}{2a} \pm \sqrt{-\frac{c}{a} + \left( \frac{b}{2a} \right)^2}$$

## Example of Completing the Square

Let's apply the method of completing the square to a specific quadratic equation:

Example Equation:

$$2x^2 + 8x - 10 = 0$$

Step 1: Divide by 2

$$x^2 + 4x - 5 = 0$$

Step 2: Move the Constant to the Right Side

$$x^2 + 4x = 5$$

Step 3: Complete the Square

Take half of 4, square it, and add to both sides:

$$\left( \frac{4}{2} \right)^2 = 4$$

So, we add 4 to both sides:

$$x^2 + 4x + 4 = 5 + 4$$

This simplifies to:

$$\sqrt{(x + 2)^2} = 9$$

Step 4: Solve for  $x$

Taking the square root of both sides:

$$x + 2 = \pm 3$$

Thus, we have two solutions:

- $x + 2 = 3 \rightarrow x = 1$
- $x + 2 = -3 \rightarrow x = -5$

So, the solutions to the original equation  $2x^2 + 8x - 10 = 0$  are  $x = 1$  and  $x = -5$ .

## Applications of Completing the Square

Completing the square is widely used in various applications, including:

### 1. Graphing Quadratic Functions

To graph a quadratic function, converting it into vertex form  $y = a(x - h)^2 + k$  using completing the square can help identify the vertex  $(h, k)$ , which is crucial for sketching the parabola.

### 2. Solving Real-World Problems

Quadratic equations often represent real-world phenomena, such as projectile motion. Completing the square can provide insights into maximum height or the time of flight.

### 3. Analyzing the Vertex and Axis of Symmetry

The vertex form obtained from completing the square allows for easy identification of the vertex and the axis of symmetry of the parabola, which is essential in optimization problems.

# Practice Problems

To solidify your understanding of completing the square, try these practice problems:

1. Complete the square for the equation  $x^2 + 6x - 7 = 0$ .
2. Solve the equation  $3x^2 - 12x + 9 = 0$  by completing the square.
3. Convert the function  $f(x) = x^2 + 8x + 15$  into vertex form.

## Conclusion

Completing the square is an essential algebraic technique that not only aids in solving quadratic equations but also enhances the understanding of quadratic functions and their properties. By mastering this method, students can approach problems with greater confidence and insight, paving the way for further studies in algebra and beyond. Through practice and application, the skill of completing the square will become a valuable tool in your mathematical toolkit.

## Frequently Asked Questions

### What is the completing the square formula in algebra?

The completing the square formula is used to transform a quadratic equation of the form  $ax^2 + bx + c$  into a perfect square trinomial, typically written as  $(x + p)^2 = q$ .

### How do you complete the square for the equation $x^2 + 6x + 5$ ?

To complete the square, take half of the coefficient of  $x$  (which is 6), square it (9), and rewrite the equation as  $(x + 3)^2 - 4$ .

### Why is completing the square useful in solving quadratic equations?

Completing the square allows us to rewrite the quadratic equation in vertex form, making it easier to identify the vertex and solve for  $x$  using the square root method.

### What steps are involved in completing the square?

1. Start with the quadratic in standard form.
2. Move the constant term to the other side.
3. Take half of the coefficient of  $x$ , square it, and add it

to both sides. 4. Factor the left side and simplify the right side.

## Can completing the square be used for any quadratic equation?

Yes, completing the square can be applied to any quadratic equation, regardless of whether it can be factored easily.

## How does completing the square relate to the quadratic formula?

Completing the square is a method that leads to the derivation of the quadratic formula, providing a systematic way to find the roots of any quadratic equation.

## What is the vertex form of a quadratic equation obtained by completing the square?

The vertex form of a quadratic equation is given by  $y = a(x - h)^2 + k$ , where  $(h, k)$  is the vertex of the parabola.

## How can you check if you have completed the square correctly?

You can verify your work by expanding the completed square and ensuring that it simplifies back to the original quadratic equation.

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