#### **Chain Rule Practice Problems**

| CHAIN RULE P                          | RACTICE PROBLEMS                       |
|---------------------------------------|--|
| Find the derivative of each. You      | do not have to simplify.               |
| $f(x) = (3x - 2)^3$                   | $f(x) = \sqrt{8x - 7}$                 |
| $f(x) = (\sin x)^3$                   | $f(x) = (\tan x)^3$                    |
| $f(x) = \left(\frac{1}{2x+3}\right)$  | $f(x) = \left(\frac{1}{3x - 4}\right)$ |
| $f(x) = \frac{1}{\sqrt[3]{5x^2 - 3}}$ | $f(x) = \frac{1}{\sqrt{6x^3 - 4}}$     |
| $f(x) = \cos 2x$                      | $f(x) = \cot 5x$                       |
| $f(x) = (5x + 7)^4$                   | $f(x) = \sqrt[5]{(7x+4)^3}$            |
| $f(x) = \sin x^5$                     | $f(x) = \tan x^5$                      |
| $f(x) = (5x + 2)^3$                   | $f(x) = \frac{2x - 5}{(2x + 1)^3}$     |
| $f(x) = x(7x + 3)^4$                  | $f(x) = (3x - 4)^3(2x + 5)^3$          |
| $f(x) = (\sin 2x)^3$                  | $f(x) = (\tan 3x)^5$                   |

Chain rule practice problems are essential for mastering calculus, particularly when it comes to differentiating composite functions. The chain rule is a fundamental concept that allows us to find the derivative of a function that is composed of other functions. Understanding how to apply the chain rule through various practice problems will not only solidify your grasp of the concept but also enhance your problem-solving skills in calculus.

Understanding the Chain Rule

The chain rule states that if you have a function (y = f(g(x))), where (f) and (g) are both differentiable functions, then the derivative of (y) with respect to (x) is given by:

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\[
\frac{dy}{dx} = f'(g(x)) \cdot g'(x)
\]
```

Components of the Chain Rule

To apply the chain rule effectively, it's important to identify the following components:

- 1. Outer Function: The function (f(y)) in the expression (f(g(x))).
- 2. Inner Function: The function  $\setminus (g \setminus)$  which is inside the outer function.
- 3. Derivatives: Calculate  $\backslash (f' \backslash)$  (the derivative of the outer function) and  $\backslash (g' \backslash)$  (the derivative of the inner function).

Basic Chain Rule Practice Problems

Let's start with some foundational problems to get familiar with the chain rule.

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Problem 1: Differentiate (y = (3x + 2)^5)
Solution Steps:
1. Identify the outer and inner functions:
- Outer function \backslash (f(u) = u^5 \backslash)
- Inner function (g(x) = 3x + 2)
2. Calculate derivatives:
- \setminus (f'(u) = 5u^4 \setminus)
- \setminus (g'(x) = 3 \setminus)
3. Apply the chain rule:
\frac{dy}{dx} = f'(g(x)) \cdot dot g'(x) = 5(3x + 2)^4 \cdot dot 3
\]
1/
\frac{dy}{dx} = 15(3x + 2)^4
\]
Problem 2: Differentiate (y = \sin(2x^2))
Solution Steps:
1. Identify the functions:
- Outer function \setminus (f(u) = \sin(u))
- Inner function (g(x) = 2x^2)
2. Calculate derivatives:
- \setminus (f'(u) = \setminus cos(u) \setminus)
- \setminus (g'(x) = 4x \setminus)
3. Apply the chain rule:
1/
\frac{dy}{dx} = f'(g(x)) \cdot dot g'(x) = \cos(2x^2) \cdot dot 4x
\]
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\frac{dy}{dx} = 4x \cos(2x^2)
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Intermediate Chain Rule Practice Problems
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Once you're comfortable with the basics, you can move on to more complex problems that involve multiple layers of functions.

Problem 3: Differentiate  $(y = e^{3x^3 + 5})$ 

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Solution Steps:
1. Identify the functions:
- Outer function \(f(u) = e^u\)
- Inner function (g(x) = 3x^3 + 5)
2. Calculate derivatives:
- \setminus (f'(u) = e^u\setminus)
- \setminus (g'(x) = 9x^2\setminus)
3. Apply the chain rule:
] /
\frac{dy}{dx} = f'(g(x)) \cdot g'(x) = e^{3x^3 + 5} \cdot g'(x)
\]
\[
\frac{dy}{dx} = 9x^2 e^{3x^3 + 5}
\]
Problem 4: Differentiate (y = \ln(5x^2 + 3x))
Solution Steps:
1. Identify the functions:
- Outer function \backslash (f(u) = \ln(u))
- Inner function (g(x) = 5x^2 + 3x)
2. Calculate derivatives:
- \setminus (f'(u) = \frac{1}{u} \setminus
- (g'(x) = 10x + 3)
3. Apply the chain rule:
\[
\frac{dy}{dx} = f'(g(x)) \cdot dot g'(x) = \frac{1}{5x^2 + 3x} \cdot dot (10x + 3)
\]
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\frac{dy}{dx} = \frac{10x + 3}{5x^2 + 3x}
\]
Advanced Chain Rule Practice Problems
Now, let's tackle some advanced problems that combine the chain rule with
other differentiation techniques.
Problem 5: Differentiate (y = \sqrt{\frac{3x^2 + 1}})
Solution Steps:
1. Identify the functions:
- Outer function (f(u) = \sqrt{u})
- Middle function (g(v) = \tan(v))
- Inner function (h(x) = 3x^2 + 1)
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2. Calculate derivatives:
- \langle f'(u) = \frac{1}{2\sqrt{u}} \rangle
- \setminus (g'(v) = \sec^2(v))
- \setminus (h'(x) = 6x \setminus)
3. Apply the chain rule:
1/
\frac{dy}{dx} = f'(g(h(x))) \cdot dot g'(h(x)) \cdot dot h'(x) =
\frac{1}{2\sqrt{3x^2 + 1}} \cdot \frac{1}{2\sqrt{3x^2 + 1}} \cdot \frac{3x^2 + 1}{2\sqrt{3x^2 + 1}} \cdot \frac{6x}{3x^2 + 1}
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1/
\frac{dy}{dx} = \frac{6x \sec^2(3x^2 + 1)}{2 \sec^2(3x^2 + 1)}
\1
Problem 6: Differentiate (y = \cos^2(4x + 1))
Solution Steps:
1. Identify the functions:
- Outer function (f(u) = u^2)
- Inner function \langle g(x) = \langle \cos(4x + 1) \rangle
2. Calculate derivatives:
- \setminus (f'(u) = 2u \setminus)
- \setminus (g'(x) = - \setminus \sin(4x + 1) \setminus \cot 4 \setminus)
3. Apply the chain rule:
\frac{dy}{dx} = f'(g(x)) \cdot dot g'(x) = 2 \cdot cos(4x + 1)(- \cdot sin(4x + 1) \cdot cdot 4)
\]
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\frac{dy}{dx} = -8\cos(4x + 1)\sin(4x + 1)
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#### Conclusion

Practicing chain rule problems is crucial for anyone looking to excel in calculus. By working through problems of varying complexity, you strengthen your understanding of the concept and enhance your ability to tackle realworld problems involving derivatives.

Tips for Mastering the Chain Rule

- 1. Break Down the Function: Always identify the inner and outer functions clearly.
- 2. Practice Regularly: Consistent practice helps in retaining the techniques.
- 3. Check Your Work: After solving, verify by checking if the derivative makes sense or if it aligns with the function's behavior.

By following these tips and practicing the problems outlined in this article, you'll be well on your way to mastering the chain rule in calculus.

### Frequently Asked Questions

#### What is the chain rule in calculus?

The chain rule is a formula for computing the derivative of the composition of two or more functions. If you have two functions, f(x) and g(x), the derivative of their composition f(g(x)) is given by f'(g(x)) g'(x).

# How do you apply the chain rule to find the derivative of $sin(x^2)$ ?

To find the derivative of  $sin(x^2)$ , let f(u) = sin(u) where  $u = x^2$ . The derivative is f'(u) = cos(u) and u' = 2x. Therefore, the derivative of  $sin(x^2)$  is  $cos(x^2)$  2x.

### What are some common mistakes when applying the chain rule?

Common mistakes include forgetting to differentiate the outer function, neglecting to multiply by the derivative of the inner function, and misapplying the order of operations.

#### Can the chain rule be applied multiple times?

Yes, the chain rule can be applied multiple times when you have a composition of functions within another composition. Each layer can be differentiated using the chain rule.

## How do you solve composite functions using the chain rule?

To solve composite functions using the chain rule, identify the outer function and the inner function, differentiate the outer function while keeping the inner function intact, then multiply by the derivative of the inner function.

# What is an example of a chain rule problem involving an exponential function?

An example is finding the derivative of  $e^{(3x)}$ . Here, the outer function is  $e^{u}$  and the inner function is u = 3x. The derivative is  $e^{(3x)}$  3.

### How does the chain rule relate to implicit differentiation?

The chain rule is essential in implicit differentiation as it allows you to differentiate equations where y is defined implicitly in terms of x. You apply the chain rule to differentiate y with respect to x.

# What resources are available for practicing chain rule problems?

Resources for practicing chain rule problems include online calculus problem solvers, educational websites like Khan Academy, and calculus textbooks that provide practice exercises and solutions.

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### **Chain Rule Practice Problems**

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