## 2 4 Practice Writing Proofs

ne:	Date:	Period:
ALGE Given: 2x - 10 = 20 Prove: x = 15	BRA PROOFS practice 1	
Statements	Reasons	
1. 2x - 10 = 20	l.	
2. 2x - 10 + 10 = 20 + 10	2.	
3. 2x = 30	3.	
$4.\frac{2x}{2} = \frac{30}{2}$	ч.	
5. x = 15	5.	
2. Given: x + 5 = 12 Prove: x = 14		
Statements	Reasons	
$L\frac{x}{2} + 5 = 12$	l.	
$2.\frac{x}{2} + 5 - 5 = 12 - 5$	2.	
$3.\frac{x}{2} = 7$	3.	
4. $\frac{x}{2} \cdot 2 = 7 \cdot 2$	4.	
5. x = 14	5.	
3. Given: 4(x + 3) = 16 Prove: x = 1	*	
Statements	Reasons	
I. 4(x + 3) = 16	l.	
2. 4x + 12 = 16	2.	
3. 4x + 12 - 12 = 16 - 12	3.	
ч, ч <sub>х</sub> = ч	ч,	
$5. \frac{4x}{4} = \frac{4}{4}$	5.	
6. x = 1	6.	

2 4 practice writing proofs is an essential aspect of learning mathematics, particularly in areas such as geometry, algebra, and calculus. Writing proofs enables students to establish the validity of mathematical statements through logical reasoning and structured argumentation. This article will explore the importance of proof writing, common proof techniques, detailed examples, and practical tips for improving your proof-writing skills.

**Understanding the Importance of Proof Writing** 

Mathematics is not just about finding answers; it is also about understanding why those answers are

correct. Proof writing serves several critical purposes:

1. Validating Mathematical Statements: Proofs provide rigorous validation for mathematical statements,

ensuring that they hold true under specified conditions.

2. Developing Logical Thinking: The process of constructing a proof enhances logical reasoning skills,

which are valuable in various fields beyond mathematics.

3. Fostering Deep Understanding: Engaging in proof writing encourages students to deepen their

understanding of concepts, rather than simply memorizing formulas or procedures.

4. Building Communication Skills: Writing proofs requires clear and precise communication, which is

crucial in both academic and professional settings.

**Common Techniques for Writing Proofs** 

There are several techniques that mathematicians commonly use when writing proofs. Each method

serves different types of statements and can be chosen based on the context of the problem.

**Direct Proof** 

A direct proof involves starting from known facts or axioms and applying logical reasoning to arrive at

the conclusion. This method is often used for proving implications and theorems.

Example: To prove that the sum of two even integers is even.

- Let \( a \) and \( b \) be two even integers.
- By definition, an even integer can be expressed as (a = 2m ) and (b = 2n ), where (m ) and (n ) are integers.
- Then the sum (a + b = 2m + 2n = 2(m+n)).
- Since \( m+n \) is an integer, \( a + b \) is even.

## **Indirect Proof (Proof by Contradiction)**

In an indirect proof, you assume the opposite of what you want to prove and show that this leads to a contradiction. This method is particularly useful for proving a statement is true by demonstrating that its negation is false.

Example: Proving that \(\sqrt{2}\) is irrational.

- Assume, for the sake of contradiction, that  $( \sqrt{2} )$  is rational. Then it can be expressed as a fraction  $( \frac{a}{b} )$  in lowest terms, where ( a ) and ( b ) are integers.
- Squaring both sides gives  $(2 = \frac{a^2}{b^2})$ , leading to  $(a^2 = 2b^2)$ .
- This implies that \( a^2 \) is even, and consequently, \( a \) must also be even (since the square of an odd number is odd).
- If \( a \) is even, we can express it as \( a =  $2k \setminus$ ) for some integer \( k \). Substituting this back gives \( (2k)^2 =  $2b^2 \setminus$ ) or \(  $4k^2 = 2b^2 \setminus$ ), leading to \(  $b^2 = 2k^2 \setminus$ ).
- This shows \( b^2 \) is even, and thus \( b \) is also even.
- This contradicts the assumption that \( a \) and \( b \) are in lowest terms (both cannot be even), hence \( \sqrt{2} \) must be irrational.

## **Proof by Induction**

Mathematical induction is a technique used to prove statements about integers. It involves two steps: the base case and the inductive step.

- 1. Base Case: Prove that the statement holds for the initial integer (usually \( n = 1 \)).
- 2. Inductive Step: Assume the statement holds for (n = k) (inductive hypothesis) and then prove it holds for (n = k + 1).

Example: Prove that the sum of the first (n) positive integers is  $(\frac{n+1}{2})$ .

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- Base Case: For (n = 1), the sum is (1 = \frac{1(1+1)}{2}), which is true.
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- Inductive Step: Assume true for (n = k):  $(1 + 2 + ... + k = \frac{k(k+1)}{2})$ .
- Show for (n = k + 1):

1

```
1 + 2 + ... + k + (k + 1) = \frac{k(k + 1)}{2} + (k + 1) = \frac{k(k + 1) + 2(k + 1)}{2} = \frac{(k + 1)(k + 1)}{2}
```

\]

- Thus, the statement holds for (n = k + 1).

## **Proof by Exhaustion**

Proof by exhaustion involves checking all possible cases to verify a statement. This method can be tedious but is effective when the number of cases is small.

Example: Proving that for any integer (n ),  $(n^2 )$  is even if (n ) is even.

- Possible cases:
- If (n = 2k) for (k = 0, 1, 2, ...), then  $(n^2 = (2k)^2 = 4k^2 = 2(2k^2))$ , which is even.
- Since all cases lead to the same conclusion, the statement is proven.

## **Practical Tips for Writing Proofs**

Writing proofs can be challenging, especially for beginners. Here are some practical tips to improve

your proof-writing skills:

- 1. Understand the Statement: Before attempting to prove a statement, ensure you deeply understand what is being claimed. Break it down into smaller parts if necessary.
- 2. Work Through Examples: Practice with various examples to become familiar with different proof techniques. The more you practice, the more intuitive the process will become.
- 3. Organize Your Thoughts: Outline your proof before writing it out in full. Identify your starting point, the logical steps needed, and the conclusion you want to reach.
- 4. Be Precise and Clear: Use clear and concise language. Avoid unnecessary jargon and ensure each step logically follows from the previous one.
- 5. Revise and Edit: After writing a proof, take the time to review and revise it. Look for any gaps in logic or unclear explanations.
- 6. Seek Feedback: Share your proofs with peers or instructors to receive constructive feedback. This can provide new insights and highlight areas for improvement.

## Conclusion

Mastering the art of writing proofs is a fundamental skill in mathematics that extends beyond the classroom. The ability to construct logical and coherent arguments is invaluable, not just in mathematics but in any field that requires critical thinking. By practicing various proof techniques and following practical tips, you can enhance your proof-writing abilities and develop a deeper understanding of mathematical concepts. Whether you are preparing for an exam or engaging in mathematical research, the skills acquired through writing proofs will serve you well throughout your academic and professional journey.

## Frequently Asked Questions

## What is the purpose of practicing writing proofs in mathematics?

Practicing writing proofs helps students develop critical thinking skills, understand mathematical concepts deeply, and learn how to construct logical arguments.

# What are the common types of proofs students practice in '2 4 practice writing proofs'?

Common types of proofs include direct proofs, indirect proofs, proof by contradiction, and mathematical induction.

## How can students improve their proof-writing skills effectively?

Students can improve their proof-writing skills by studying examples, practicing regularly, seeking feedback, and collaborating with peers.

## What role does understanding definitions play in writing proofs?

Understanding definitions is crucial in writing proofs as it ensures that students accurately apply concepts and construct valid arguments based on precise terminology.

## What strategies can be used when starting to write a proof?

Strategies include restating the theorem, identifying known information, considering special cases, and outlining the proof structure before writing it in full.

## Why is it important to clearly state assumptions in a proof?

Clearly stating assumptions is important because it provides a foundation for the logical reasoning in the proof and clarifies the context for the argument.

## How can visualization aid in writing mathematical proofs?

Visualization can aid in writing proofs by helping students grasp complex relationships, identify patterns, and conceptualize the problem more clearly.

## What is a common mistake to avoid when writing proofs?

A common mistake to avoid is assuming that the reader understands implied steps; each step should be clearly justified to maintain logical flow.

## How does collaborative proof writing benefit students?

Collaborative proof writing benefits students by allowing them to share ideas, clarify misunderstandings, and gain new perspectives on problem-solving techniques.

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