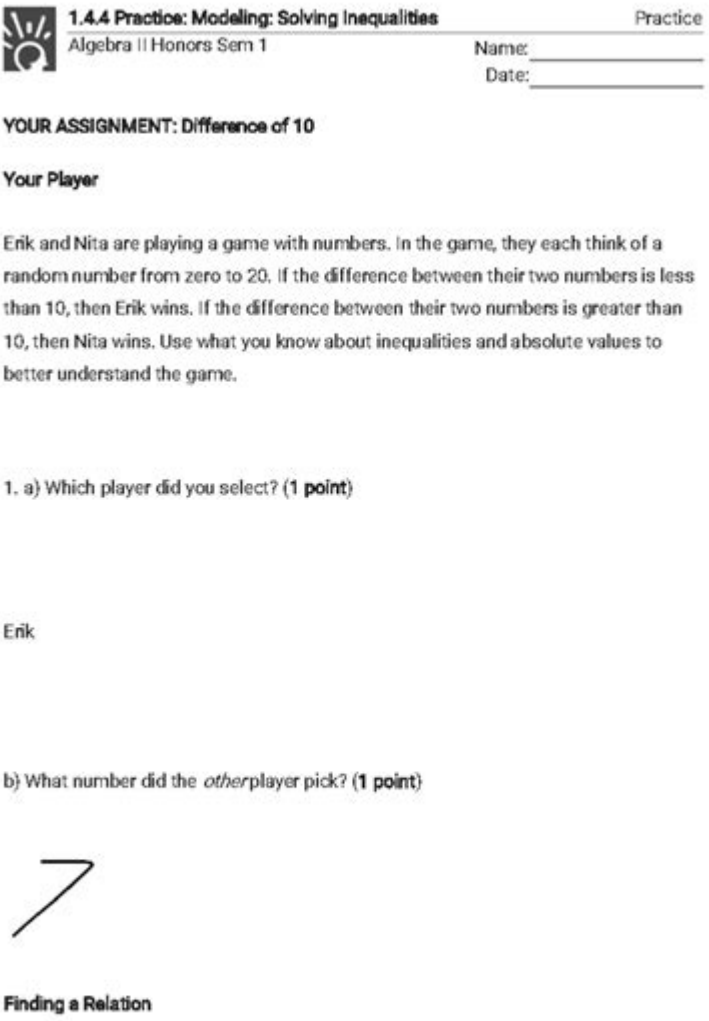
14 4 Practice Modeling Solving Inequalities



1.4.4 Practice: Modeling: Solving Inequalities — Practice
Algebra II Honors Sem 1
Name: _____
Date: _____

YOUR ASSIGNMENT: Difference of 10

Your Player

Erik and Nita are playing a game with numbers. In the game, they each think of a random number from zero to 20. If the difference between their two numbers is less than 10, then Erik wins. If the difference between their two numbers is greater than 10, then Nita wins. Use what you know about inequalities and absolute values to better understand the game.

1. a) Which player did you select? (**1 point**)

Erik

b) What number did the *other* player pick? (**1 point**)

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Finding a Relation

14 4 practice modeling solving inequalities is an essential aspect of mathematics that helps students understand how to express relationships between quantities and solve problems involving inequalities. Inequalities are mathematical expressions that show the relationship between two values that are not necessarily equal. They are fundamental in various fields, including economics, engineering, and science, as they allow for the modeling of constraints and conditions in real-world scenarios. This article will explore the concept of inequalities, their types, methods for solving them, and practical applications.

Understanding Inequalities

Inequalities are expressions that indicate that one quantity is less than, greater than, less than or equal to, or

greater than or equal to another quantity. The symbols used to denote inequalities are as follows:

- **<** (less than)
- **>** (greater than)
- **<=** (less than or equal to)
- **>=** (greater than or equal to)

For example, if we have the inequality $x > 3$, it means that x can take any value greater than 3, but not equal to 3.

Types of Inequalities

There are several types of inequalities that one may encounter in mathematics:

1. Linear Inequalities: These are inequalities involving linear expressions. For example, $2x + 3 < 7$ is a linear inequality.

2. Quadratic Inequalities: These involve quadratic expressions, such as $x^2 - 4x > 0$.

3. Polynomial Inequalities: These consist of polynomial expressions of degree higher than two.

4. Rational Inequalities: These involve ratios of polynomials. For example, $\frac{x + 1}{x - 2} \geq 0$.

5. Absolute Value Inequalities: These involve absolute values, such as $|x - 5| < 3$.

Solving Inequalities

Solving inequalities involves finding the values of the variable that satisfy the given inequality. The methods for solving inequalities can vary depending on the type but generally follow a systematic approach.

Step-by-Step Method for Solving Linear Inequalities

1. Isolate the variable: The first step is to get the variable on one side of the inequality while moving the constants to the other side. For example, for the inequality $2x + 3 < 7$, subtract 3 from both sides to get $2x < 4$.

2. Divide or multiply: If the variable is multiplied by a coefficient, divide both sides by that coefficient. If

the coefficient is negative, remember to flip the inequality sign. Continuing with the previous example, divide both sides by 2 to find $x < 2$.

3. Graph the solution: Represent the solution on a number line. For $x < 2$, you would draw an open circle at 2 and shade the line to the left to indicate all numbers less than 2.

Examples of Solving Different Types of Inequalities

1. Linear Inequality: Solve $4x - 5 \geq 3$.
- Add 5 to both sides: $4x \geq 8$.
- Divide by 4: $x \geq 2$.
- Solution: x includes 2 and all values greater than 2.

2. Quadratic Inequality: Solve $x^2 - x - 6 < 0$.
- Factor the quadratic: $(x - 3)(x + 2) < 0$.
- Find the critical points: $x = 3$ and $x = -2$.
- Test intervals:
- For $x < -2$, choose $x = -3$: $(-)(-) > 0$ (not a solution).
- For $-2 < x < 3$, choose $x = 0$: $(-)(+) < 0$ (solution).
- For $x > 3$, choose $x = 4$: $(+)(+) > 0$ (not a solution).
- Solution: $-2 < x < 3$.

3. Absolute Value Inequality: Solve $|x - 4| < 2$.
- Rewrite as two inequalities: $-2 < x - 4 < 2$.
- Solve each part:
- From $-2 < x - 4$: $x > 2$.
- From $x - 4 < 2$: $x < 6$.
- Solution: $2 < x < 6$.

Graphing Solutions to Inequalities

Graphing inequalities on a number line or coordinate plane helps visualize the solutions.

- Number Line: Use open circles for inequalities that do not include the endpoint (e.g., $<$ or $>$) and closed circles for inequalities that do include the endpoint (e.g., $\leq$ or $\geq$).

- Coordinate Plane: For linear inequalities in two variables (e.g., $y < 2x + 1$), graph the corresponding line (using a dashed line for $<$ or $>$ and a solid line for $\leq$ or $\geq$). Then, shade the region that satisfies the inequality.

Applications of Inequalities

Inequalities are used in various real-world situations, including:

1. Economics: Inequalities can represent budget constraints, such as $3x + 2y \leq 30$, where x and y are quantities of goods.

2. Engineering: Inequalities help in design specifications and safety margins, ensuring that certain parameters are maintained within a safe range.

3. Statistics: Inequalities are used in hypothesis testing to determine confidence intervals and significance levels.

4. Optimization Problems: Many optimization problems involve inequalities to constrain resources or requirements, such as maximizing profit while adhering to cost limits.

Conclusion

In conclusion, understanding and solving inequalities is a vital skill in mathematics that extends beyond the classroom into various professional fields. By mastering the techniques for solving different types of inequalities, students can effectively model and analyze real-world problems. The ability to graph inequalities also enhances comprehension and visualization, making it easier to communicate solutions. As we continue to explore the vast world of mathematics, the role of inequalities will undoubtedly remain significant in shaping our understanding of relationships and constraints.

Frequently Asked Questions

What is the primary goal of solving inequalities in algebra?

The primary goal is to find the set of values that satisfy the inequality, which can often be represented as a range of numbers on a number line.

How do you graph the solution of a linear inequality?

To graph a linear inequality, first graph the corresponding equation as a solid line if it's '≤' or '≥' and as a dashed line if it's '<' or '>'. Then, shade the region that represents the solution set.

What are the steps involved in solving a two-step inequality?

The steps include isolating the variable by performing inverse operations, similar to solving an equation, while remembering to reverse the inequality sign when multiplying or dividing by a negative number.

Can you provide an example of a compound inequality?

An example of a compound inequality is '3 < x + 2 < 7', which means you need to solve both inequalities: 'x + 2 > 3' and 'x + 2 < 7'.

What does it mean when an inequality has no solution?

An inequality has no solution when the conditions cannot be satisfied, such as when the inequality leads to a false statement like '5 < 3'.

How can absolute value inequalities be solved?

Absolute value inequalities are solved by splitting them into two separate inequalities, one for the positive case and one for the negative case, then solving each inequality individually.

What is the significance of the solution set in an inequality?

The solution set represents all possible values that satisfy the inequality, providing a range of solutions rather than a single value, which is crucial in real-world applications.

How do you check your solution for an inequality?

To check your solution, substitute a value from the solution set back into the original inequality to see if the inequality holds true, confirming that the solution is correct.

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